

Situation Calculus-based Online Plan Recognition in Continuous Domains

Christoph Schwering

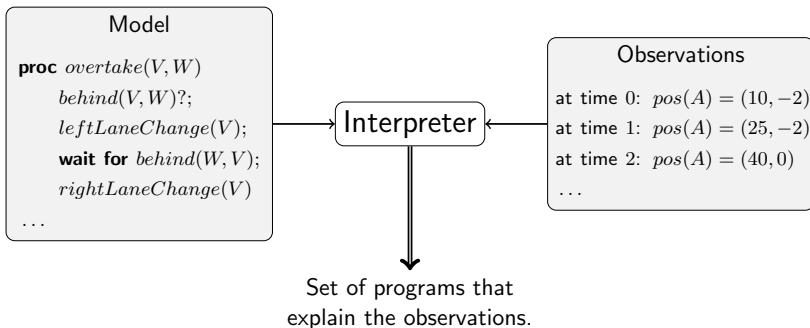
RWTH Aachen University

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Motivation



Approach



Outline

Introduction

- Related Work
- Modeling

Semantics

- Time and Continuous Change
- Multiple Agents
- Robustness

Plan Recognition by Program Execution

- observe* Actions
- Online Heuristic

Evaluation

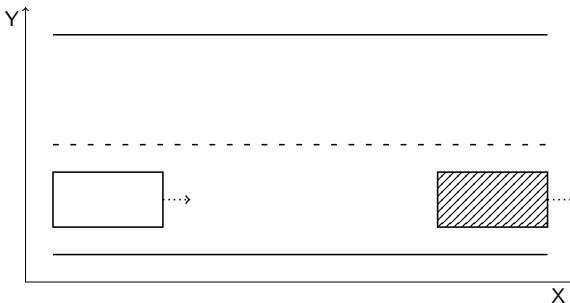
Discussion

Related Work

	Kautz and Allen [1986]	Charniak and Goldman [1991]	Goultiaeva and Lespérance [2006]
Plans	consistent	likely	consistent
Tools	circumscription	Bayesian network	situation calculus
Modeling	first-order logic		ConGolog
Focus	abstraction		abstraction, online
Observations	primitive action occurrences		

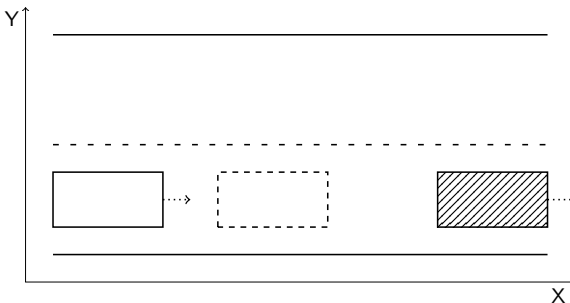
Bui et al. [2002]	Geib and Goldman [2009]	Ramirez and Geffner [2009]
likely	likely	consistent/likely
HMM	HMM	planner
hierarchical MDPs	plan tree grammars	STRIPS, goal library
abstraction, uncertainty	abstraction, partial ordering	–
primitive action occurrences		

Modeling



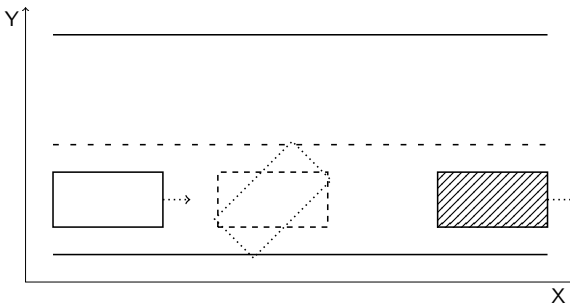
- ▶ Global cartesian view
- ▶ Vehicle = rectangle
- ▶ Instantaneous actions *setYaw*, *setVeloc*

Modeling



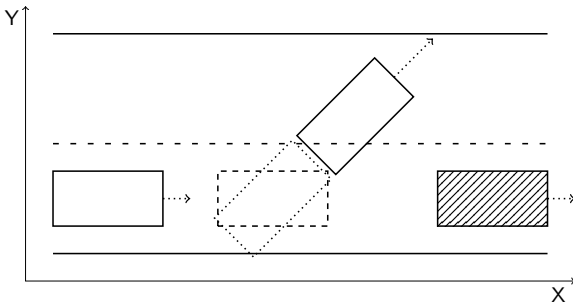
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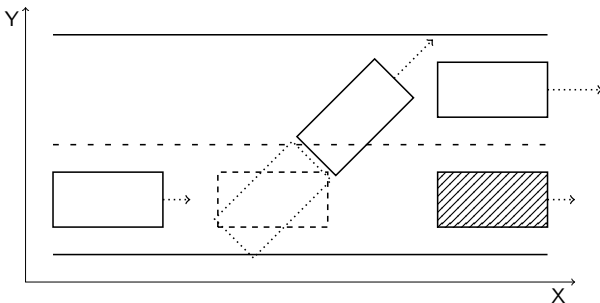
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Modeling



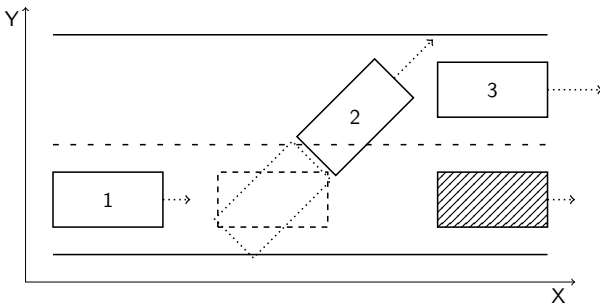
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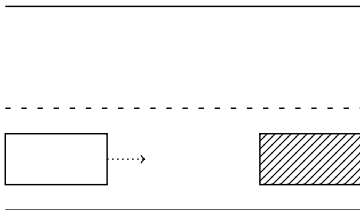
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Modeling



- ▶ Global cartesian view
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Programs

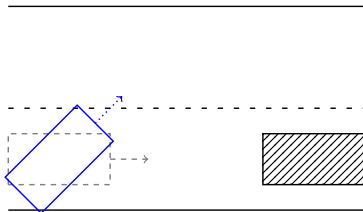


```

proc leftLaneChange(V)
  pick  $\gamma \in \{4^\circ, 6^\circ, \dots, 12^\circ\}$  do
    setYaw(V,  $\gamma$ )
  endpick;
  onRightLane(V) ?;
  % time passes indefinitely
  setYaw(V,  $0^\circ$ );
  onLeftLane(V) ?
endproc

```

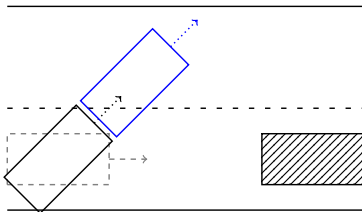
Programs



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Programs

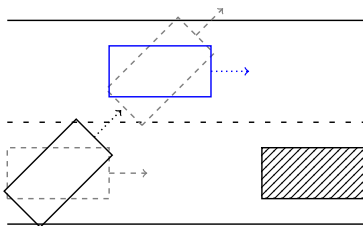


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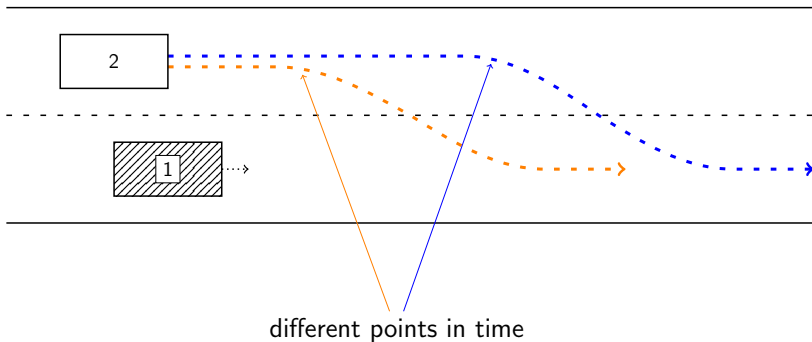
Semantics

What is needed to make it work?

Golog *Trans* +

- ▶ Flexible timing
- ▶ Continuous change
- ▶ Multi-agent
- ▶ Robustness

Time and Continuous Change



Time and Continuous Change

From temporal sequential Golog:

$$time(A(\vec{x}, \tau)) = \tau$$

$$start(do(a, s)) = time(a)$$

From cc-Golog:

$\phi[s, \tau]$ evaluate ϕ in s at time τ

$\alpha[s, \tau]$ append new time parameter
e.g. $jump[s, \tau] = jump(\tau)$

Time and Continuous Change

primitive action

$$\begin{aligned} Trans(\overset{\swarrow}{\alpha}, s, \delta, s') &\equiv \delta = Nil \wedge \\ &\quad \exists \tau. \tau \geq start(s) \wedge \\ &\quad Poss(\alpha[s, \tau], s) \wedge \\ &\quad s' = do(\alpha[s, \tau], s) \end{aligned}$$

Time and Continuous Change

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monotonicity

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Time and Continuous Change

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$$Trans(\alpha, s, \delta, s') \equiv \delta = Nil \wedge$$
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constrains τ further

$$Poss(\alpha[s, \tau], s) \wedge$$
$$s' = do(\alpha[s, \tau], s)$$

The diagram illustrates the definition of the Trans predicate. It consists of three lines of mathematical expressions. The first line is $Trans(\alpha, s, \delta, s') \equiv \delta = Nil \wedge$. The second line is $\exists \tau. \tau \geq start(s) \wedge$. The third line is $Poss(\alpha[s, \tau], s) \wedge$. The fourth line is $s' = do(\alpha[s, \tau], s)$. Annotations include: 'primitive action' with an arrow pointing to α ; 'monotonicity' with an arrow pointing to $start(s)$; and 'constrains τ further' with a curved arrow pointing from the text to $\alpha[s, \tau]$.

Time and Continuous Change

primitive action

monotonicity

$$Trans(\alpha, s, \delta, s') \equiv \delta = Nil \wedge \exists \tau. \tau \geq start(s) \wedge$$

constrains τ further

advance to time τ

$$Poss(\alpha[s, \tau], s) \wedge s' = do(\alpha[s, \tau], s)$$

Time and Continuous Change

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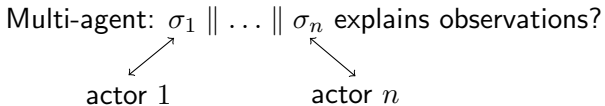
advance to time τ

$$Poss(\alpha[s, \tau], s) \wedge$$

$$s' = do(\alpha[s, \tau], s)$$

$$Poss(waitFor(\phi, \tau), s) \equiv \phi[s, \tau]$$

Multiple Agents



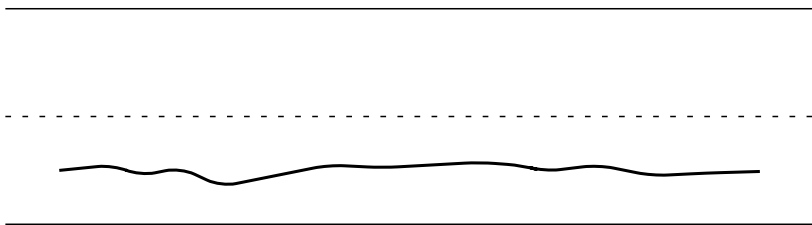
Multiple Agents

Multi-agent: $\sigma_1 \parallel \dots \parallel \sigma_n$ explains observations?
↙ ↘
actor 1 actor n

Concurrency as in ConGolog:

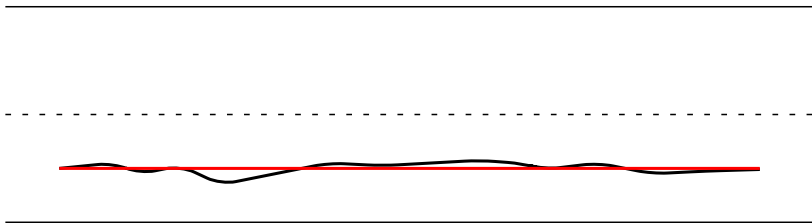
$$\begin{aligned} \text{Trans}(\sigma_1 \parallel \sigma_2, s, \delta, s') &\equiv \exists \delta' . \text{Trans}(\sigma_1, s, \delta', s') \wedge \delta = \delta' \parallel \sigma_2 \vee \\ &\quad \exists \delta' . \text{Trans}(\sigma_2, s, \delta', s') \wedge \delta = \sigma_1 \parallel \delta' \end{aligned}$$

Robustness



Observed trace

Robustness

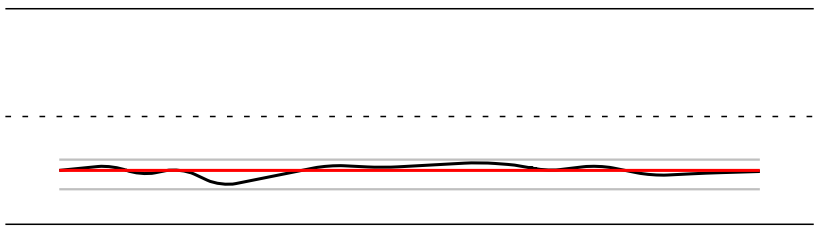


Observed trace + model trace



Hypothesis: driving straight?

Robustness



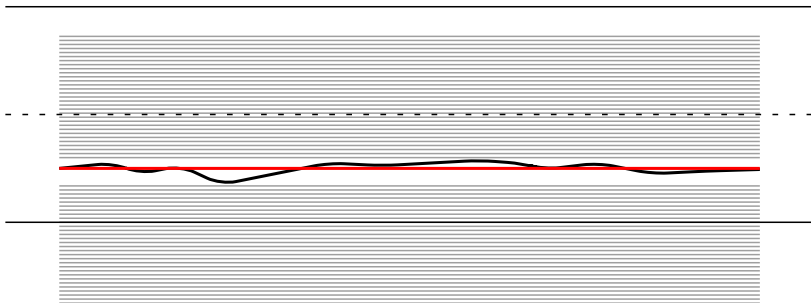
Observed trace + **model trace** +

lateral tolerance



Hypothesis: driving straight?

Robustness

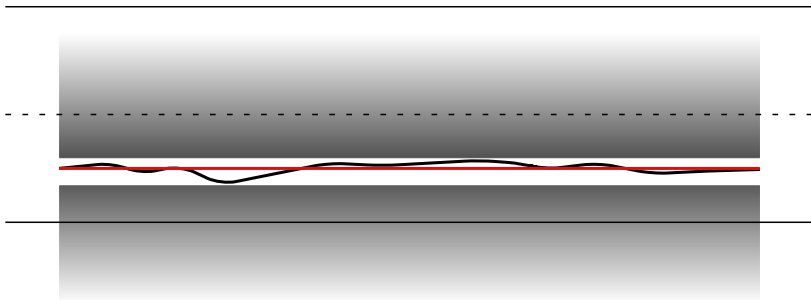


Observed trace + model trace +

lateral tolerances

↑
Hypothesis: driving straight?

Robustness

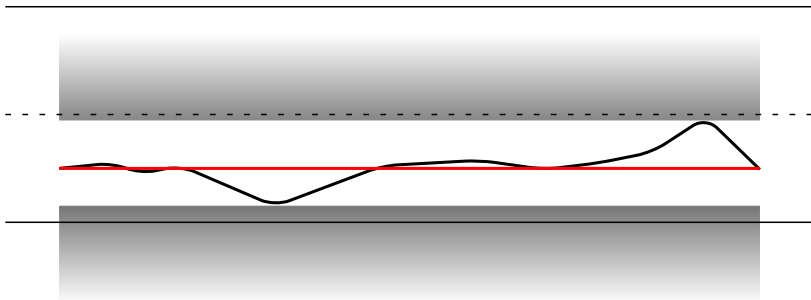


Observed trace + model trace + weighted lateral tolerances



Hypothesis: driving straight? **Likely**

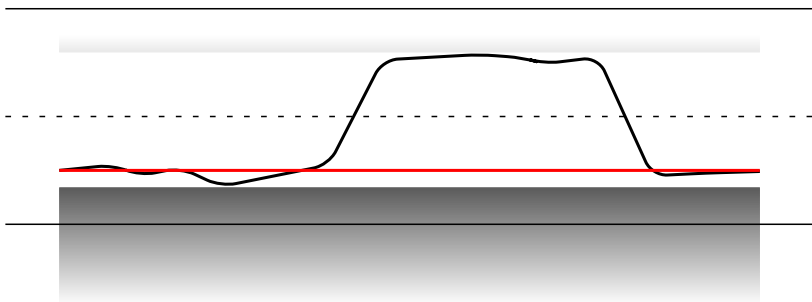
Robustness



Observed trace + model trace + weighted lateral tolerances

Hypothesis: driving straight? **Less likely**

Robustness



Observed trace + model trace + weighted lateral tolerances

Hypothesis: driving straight? **Unlikely**

Robustness

- ▶ Tolerances by stochastic actions
 $Choice(\beta, \alpha)$ and $prob_0(\beta, \alpha, s) \mapsto [0, 1]$

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 $Choice(\beta, \alpha)$ and $prob_0(\beta, \alpha, s) \mapsto [0, 1]$
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$$r(s) \mapsto \mathbb{R}$$

} user-supplied

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- ▶ Nondeterminism → choose **best alternative**

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- ▶ Nondeterminism \rightarrow choose **best alternative**:
 1. Decompose σ into $(\gamma; \delta)$ *atomic* action
 2. Find **best** $(\gamma; \delta)$ amongst all decompositions
 3. Execute γ

Robustness

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 $Choice(\beta, \alpha)$ and $prob_0(\beta, \alpha, s) \mapsto [0, 1]$
- ▶ Rate **situation** by reward

$$r(s) \mapsto \mathbb{R}$$

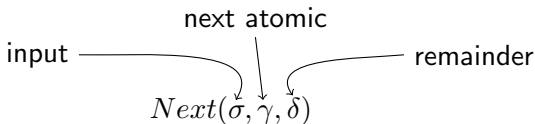
} user-supplied

- ▶ Rate **program** by estimated reward

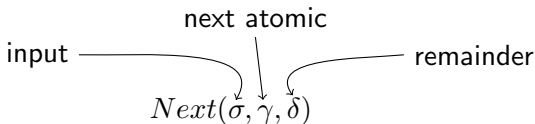
$$value(r, \sigma, s) \mapsto \mathbb{R}$$

- ▶ Nondeterminism \rightarrow choose **best alternative**:
 1. Decompose σ into $(\gamma; \delta)$ **atomic** action
 2. Find **best** $(\gamma; \delta)$ amongst all decompositions
 3. Execute γ

Robustness: Decomposition



Robustness: Decomposition



Like *Trans* without execution, e.g.:

$$Next(\alpha, \gamma, \delta) \equiv \gamma = \alpha \wedge \delta = Nil$$

$$Next(\sigma_1 | \sigma_2, \gamma, \delta) \equiv Next(\sigma_1, \gamma, \delta) \vee Next(\sigma_2, \gamma, \delta)$$

Robustness: Transition

$$\begin{aligned}
 & \text{transPr}(r, \sigma, s, \delta, s') = p \equiv \\
 & \text{if } \exists^1 \gamma_1, \delta_1 . \text{Next}(\sigma, \gamma_1, \delta_1) \wedge \\
 & \quad (\forall \gamma_2, \delta_2 . \text{Next}(\sigma, \gamma_2, \delta_2) \supset \text{value}(r, (\gamma_1; \delta_1), s) \geq \text{value}(r, (\gamma_2; \delta_2), s)) \\
 & \quad \text{then (if } \delta = \delta_1 \text{ then } p = \text{transAtPr}(r, \gamma_1, \delta_1, s, s') \text{ else } p = 0) \\
 & \text{else } p = 0
 \end{aligned}$$

decomposition $\gamma_1; \delta_1$ is optimal

execute γ_1

Robustness

Why decomposition? Decision theory + concurrency

Trans recursively follows syntax tree
↪ does not know “what comes after”

Robustness

Why decomposition? Decision theory + concurrency

Trans recursively follows syntax tree
~> does not know “what comes after”

Program decomposition

~> full remaining program is always known

~> can resolve nondeterminism with remainder in mind

Robustness: Atomic Complex Actions

$$\begin{aligned} \text{atomic}(a; b) \parallel c &\not\sim do([a, c, b], S_0) \\ &\rightsquigarrow do([a, b, c], S_0) \\ &\rightsquigarrow do([c, a, b], S_0) \end{aligned}$$

Plan Recognition by Program Execution

Plan recognition...

- ▶ as satisfiability
- ▶ by iterative filtering of *allConsistPlans*
- ▶ by program execution

Plan Recognition by Program Execution

Plan recognition...

- ▶ as satisfiability
- ▶ by iterative filtering of *allConsistPlans*
- ▶ by **program execution**

equivalent



observe Actions

$$Poss(\textit{observe}(\tau, \phi, \tau'), s) \equiv \tau = \tau' \wedge \phi[s, \tau]$$

Execution of $\textit{observe}(\tau, \phi)$ means ϕ was observed at time τ

observe Actions

$$Poss(\textit{observe}(\tau, \phi, \tau'), s) \equiv \tau = \tau' \wedge \phi[s, \tau]$$

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$$(\textit{observe}(\tau_1, \phi_1); \dots; \textit{observe}(\tau_n, \phi_n))$$

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Execution of $\text{observe}(\tau, \phi)$ means ϕ was observed at time τ

$$\sigma \quad (\text{observe}(\tau_1, \phi_1); \dots; \text{observe}(\tau_n, \phi_n))$$

observe Actions

$$Poss(\textit{observe}(\tau, \phi, \tau'), s) \equiv \tau = \tau' \wedge \phi[s, \tau]$$

Execution of $\textit{observe}(\tau, \phi)$ means ϕ was observed at time τ

$$\sigma \quad || \quad (\textit{observe}(\tau_1, \phi_1); \dots; \textit{observe}(\tau_n, \phi_n))$$

Online Heuristic

1. New observation (τ, ϕ) present:

$$\delta' = \delta \parallel \text{observe}(\tau, \phi)$$

← merge observation

Online Heuristic

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2. Enough *observe* actions buffered:

$$p' = p \cdot \text{transPr}(r, \delta, s, \delta', s')$$

resolves nondeterminism

Online Heuristic

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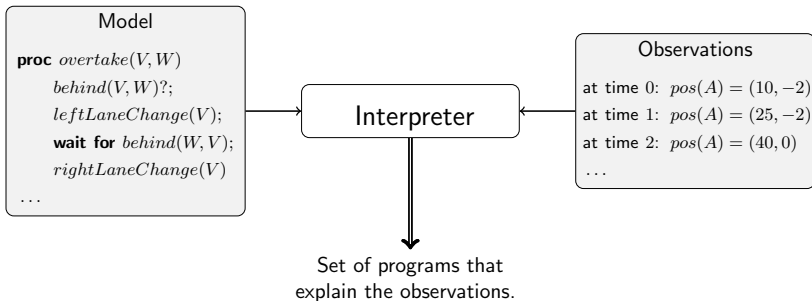
2. Enough *observe* actions buffered:

$$p' = p \cdot \text{transPr}(r, \delta, s, \delta', s')$$

← resolves nondeterminism

3. Reiterate.

Approach Summary



Approach Summary

Candidate programs of the form

$$\sigma_1 \parallel \dots \parallel \sigma_n$$

for n actors.

Model

```
proc overtake(V, W)
  behind(V, W)?;
  leftLaneChange(V);
  wait for behind(W, V);
  rightLaneChange(V)
...
```

Interpreter

Set of programs that explain the observations.

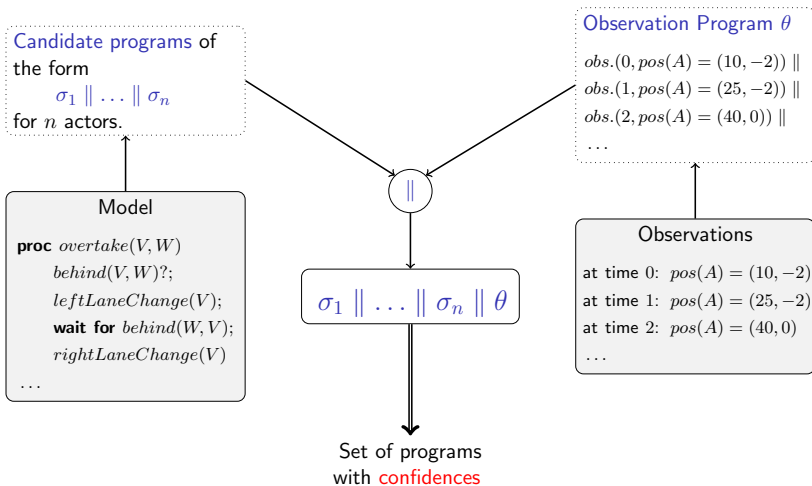
Observation Program θ

```
obs.(0, pos(A) = (10, -2)) ||
obs.(1, pos(A) = (25, -2)) ||
obs.(2, pos(A) = (40, 0)) ||
...
```

Observations

```
at time 0: pos(A) = (10, -2)
at time 1: pos(A) = (25, -2)
at time 2: pos(A) = (40, 0)
...
```

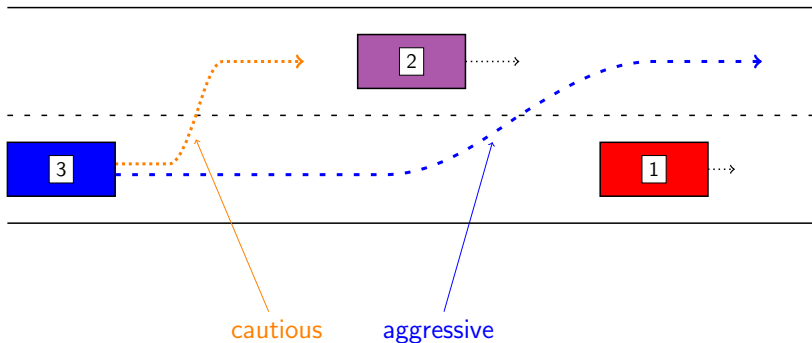
Approach Summary



Evaluation

- ▶ Prototype in ECLiPSe-CLP
- ▶ Sampling
- ▶ Linear constraint solver
for equations from *waitFor*, *observe*

Demo



Video #1 Video #2

Conclusion

Accomplishments

- ✓ Flexible timing
- ✓ Continuous change
- ✓ Multi-agent
- ✓ Robustness
 - Model simplifies world

Conclusion

Plan Recognition by Program Execution

Accomplishments

- ✓ Flexible timing
- ✓ Continuous change
- ✓ Multi-agent
- ✓ Robustness
 - Model simplifies world
 - Sensor noise

Features

- ▶ Keeps it simple
- ▶ Sensor noise
- ▶ Efficient

Future Work

- ▶ Nonlinear constraints
- ▶ Extrapolate situation + remaining program

Appendix

Bibliography

- Hung H. Bui, Svetha Venkatesh, and Geoff West. Policy recognition in the abstract hidden markov model. *Journal of Artificial Intelligence Research*, 17:2002, 2002.
- Eugene Charniak and Robert Goldman. A probabilistic model of plan recognition. In *Proceedings of the ninth National conference on Artificial Intelligence*, volume 1 of *AAAI'91*, pages 160–165. AAAI Press, 1991.
- Christopher Geib and Robert Goldman. A probabilistic plan recognition algorithm based on plan tree grammars. *Artificial Intelligence*, 173: 1101–1132, 2009.
- Alexandra Goultiaeva and Yves Lespérance. Incremental plan recognition in an agent programming framework. In *Cognitive Robotics Workshop*, pages 83–90, 2006.
- Henry A. Kautz and James F. Allen. Generalized plan recognition. In *Proceedings of the Fifth National Conference on Artificial Intelligence*, pages 32–37, 1986.
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User Guarantees

The axiomizer must guarantee:

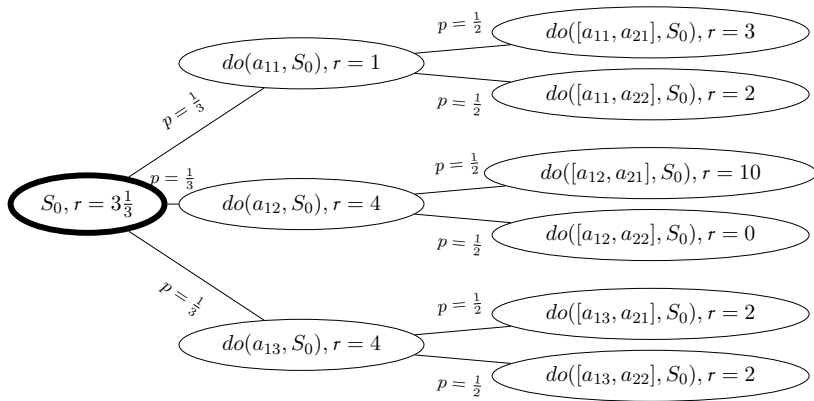
$$\mathcal{D} \models \text{Choice}(\beta, \alpha) \wedge (\exists \tau . \tau \geq \text{start}(s) \wedge \text{Poss}(\alpha[s, \tau], s)) \supset \\ \text{prob}_0(\beta, \alpha, s) > 0$$

$$\mathcal{D} \models (\exists \alpha . \text{Choice}(\beta, \alpha) \wedge \exists \tau . \tau \geq \text{start}(s) \wedge \text{Poss}(\alpha[s, \tau], s)) \supset \\ \sum_{\{\alpha \mid \text{Choice}(\beta, \alpha) \wedge \\ \exists \tau . \tau \geq \text{start}(s) \wedge \\ \text{Poss}(\alpha[s, \tau], s)\}} \text{prob}_0(\beta, \alpha, s) = 1$$

$$\mathcal{D} \models \forall \beta . \exists f . \forall \alpha . \text{Choice}(\beta, \alpha) \supset (\exists i) f(i) = \alpha$$

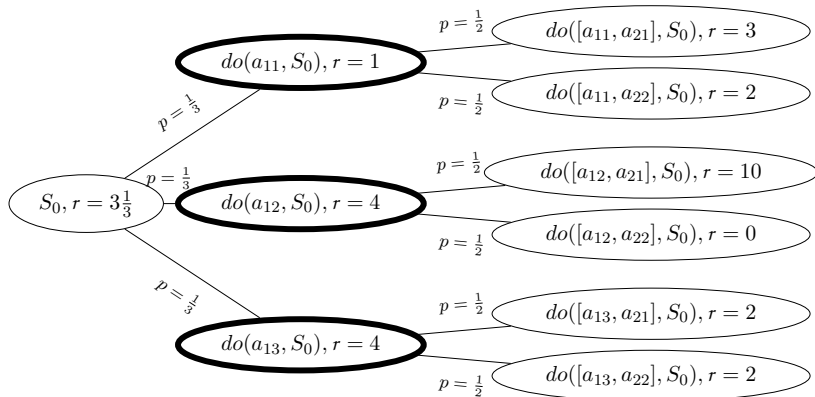
Robustness: *value*

$$\text{value}(r, \sigma, S_0) \geq 3\frac{1}{3}$$



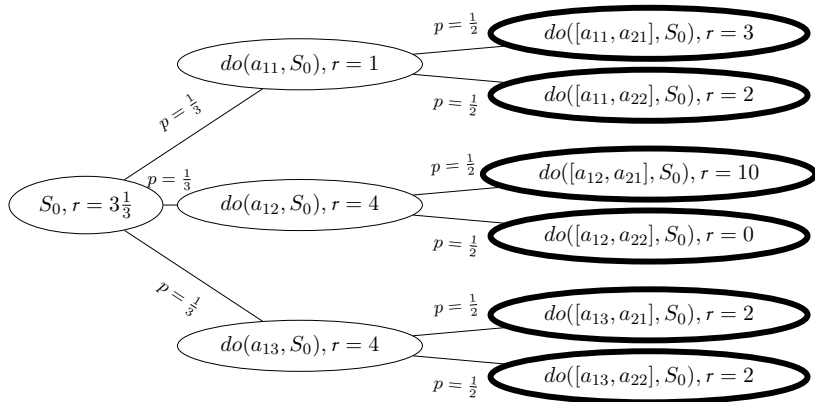
Robustness: *value*

$$value(r, \sigma, S_0) \geq 3$$



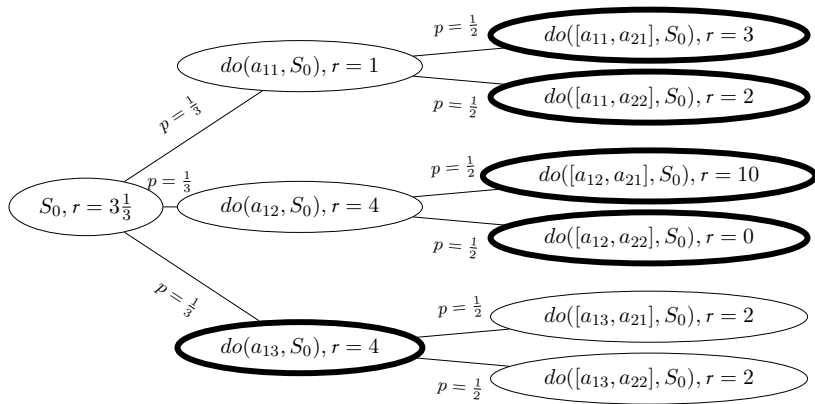
Robustness: *value*

$$\text{value}(r, \sigma, S_0) \geq 3\frac{1}{6}$$



Robustness: *value*

$$\text{value}(r, \sigma, S_0) = 3\frac{5}{6}$$



Robustness: *value*

$$\begin{aligned}
 \text{Best}(r, \sigma, s) &\stackrel{\text{def}}{=} \forall P. (\forall s', s''. P(s') \wedge P(s'') \supset s' \not\sqsubseteq s'') \supset \\
 &\quad \sum_{\{(p, s') \mid \exists \delta. \text{transPr}^*(r, \sigma, s, \delta, s') = p \wedge \\
 &\quad p > 0 \wedge P(s')\}} p \cdot r(s') \leq r(s)
 \end{aligned}$$

$$\begin{aligned}
 \text{value}(r, \sigma, s) &\stackrel{\text{def}}{=} \sum_{\{(p, s') \mid \exists \delta. \text{transPr}^*(r, \sigma, s, \delta, s') = p \wedge \\
 &\quad p > 0 \wedge \text{Best}(r, \delta, s') \wedge \\
 &\quad \neg \exists s'', \delta. \text{transPr}^*(r, \sigma, s, \delta, s'') > 0 \wedge \\
 &\quad \text{Best}(r, \delta, s'') \wedge s'' \sqsubset s'\}} p \cdot r(s')
 \end{aligned}$$

Robustness: Sum Axiomatization

$$\sum_{\{\vec{x} \mid \Phi[\vec{X}/\vec{x}]\}} \nu(\vec{x})$$

$$\text{sum}_\nu(\Phi(\vec{X})) = v \stackrel{\text{def}}{=} \exists f, g.$$

$$(\forall \vec{x}) (\Phi[\vec{X}/\vec{x}] \supset (\exists i) \vec{x} = g(i)) \wedge$$

$$(\forall i, j) (\Phi[\vec{X}/g(i)] \wedge \Phi[\vec{X}/g(j)] \wedge i \neq j \supset g(i) \neq g(j)) \wedge$$

$$f(0) = 0 \wedge$$

$$(\forall i) ((\Phi[\vec{X}/g(i)] \supset f(i+1) = f(i) + \nu(g(i))) \wedge$$

$$(\neg \Phi[\vec{X}/g(i)] \supset f(i+1) = f(i))) \wedge$$

$$(\forall i) (f(i) \leq v \wedge$$

$$(\forall v') (f(i) \leq v' \supset v \leq v'))$$

Robustness: *Next*

$$\text{Next}(\text{Nil}, \gamma, \delta) \equiv \text{False}$$

$$\text{Next}(\alpha, \gamma, \delta) \equiv \gamma = \alpha \wedge \delta = \text{Nil}$$

$$\text{Next}(\beta, \gamma, \delta) \equiv \gamma = \beta \wedge \delta = \text{Nil}$$

$$\text{Next}(\phi?, \gamma, \delta) \equiv \gamma = \phi? \wedge \delta = \text{Nil}$$

$$\text{Next}(\pi v . \sigma, \gamma, \delta) \equiv \exists x . \text{Next}(\sigma_x^v, \gamma, \delta)$$

$$\text{Next}(\sigma_1 \mid \sigma_2, \gamma, \delta) \equiv \text{Next}(\sigma_1, \gamma, \delta) \vee \text{Next}(\sigma_2, \gamma, \delta)$$

$$\begin{aligned} \text{Next}(\sigma_1; \sigma_2, \gamma, \delta) \equiv & \exists \sigma'_1 . \text{Next}(\sigma_1, \gamma, \sigma'_1) \wedge \delta = \sigma'_1; \sigma_2 \vee \\ & \text{MaybeFinal}(\sigma_1) \wedge \text{Next}(\sigma_2, \gamma, \delta) \end{aligned}$$

$$\begin{aligned} \text{Next}(\sigma_1 \parallel \sigma_2, \gamma, \delta) \equiv & \exists \sigma'_1 . \text{Next}(\sigma_1, \gamma, \sigma'_1) \wedge \delta = \sigma'_1 \parallel \sigma_2 \vee \\ & \exists \sigma'_2 . \text{Next}(\sigma_2, \gamma, \sigma'_2) \wedge \delta = \sigma_1 \parallel \sigma'_2 \end{aligned}$$

$$\text{Next}(\sigma^*, \gamma, \delta) \equiv \exists \sigma' . \text{Next}(\sigma, \gamma, \sigma') \wedge \delta = \sigma'; \sigma^*$$

Robustness: *MaybeFinal*

$$\textit{MaybeFinal}(\textit{Nil}) \equiv \textit{True}$$

$$\textit{MaybeFinal}(\alpha) \equiv \textit{False}$$

$$\textit{MaybeFinal}(\beta) \equiv \textit{False}$$

$$\textit{MaybeFinal}(\phi?) \equiv \textit{False}$$

$$\textit{MaybeFinal}(\pi v . \sigma) \equiv \exists x . \textit{MaybeFinal}(\sigma_x^v)$$

$$\textit{MaybeFinal}(\sigma_1 \mid \sigma_2) \equiv \textit{MaybeFinal}(\sigma_1) \vee \textit{MaybeFinal}(\sigma_2)$$

$$\textit{MaybeFinal}(\sigma_1; \sigma_2) \equiv \textit{MaybeFinal}(\sigma_1) \wedge \textit{MaybeFinal}(\sigma_2)$$

$$\textit{MaybeFinal}(\sigma_1 \parallel \sigma_2) \equiv \textit{MaybeFinal}(\sigma_1) \wedge \textit{MaybeFinal}(\sigma_2)$$

$$\textit{MaybeFinal}(\sigma^*) \equiv \textit{True}$$

Robustness: *transAtPr*

$transAtPr(r, \alpha, \delta, s, s') = p \equiv$

if $\exists^1 \tau . \tau \geq start(s) \wedge Poss(\alpha[s, \tau], s) \wedge s' = do(\alpha[s, \tau], s)$

then $p = 1$ **else** $p = 0$

Robustness: $transAtPr$

$transAtPr(r, \alpha, \delta, s, s') = p \equiv$

if $\exists^1 \tau . \tau \geq start(s) \wedge Poss(\alpha[s, \tau], s) \wedge s' = do(\alpha[s, \tau], s) \wedge$
 $(\forall \tau', s'' . \tau' \geq start(s) \wedge Poss(\alpha[s, \tau'], s) \wedge s'' = do(\alpha[s, \tau'], s) \supset$
 $value(r, \delta, s') \geq value(r, \delta, s''))$

then $p = 1$ **else** $p = 0$

Annotations:

- rest program (points to δ)
- choose r -maximizing τ (points to the comparison in the if condition)

Robustness: $transAtPr$

rest program

$$transAtPr(r, \alpha, \delta, s, s') = p \equiv$$

if $\exists^1 \tau . \tau \geq start(s) \wedge Poss(\alpha[s, \tau], s) \wedge s' = do(\alpha[s, \tau], s) \wedge$
 $(\forall \tau', s'' . \tau' \geq start(s) \wedge Poss(\alpha[s, \tau'], s) \wedge s'' = do(\alpha[s, \tau'], s) \supset$
 $value(r, \delta, s') \geq value(r, \delta, s''))$
then $p = 1$ **else** $p = 0$

choose r -maximizing τ

$$transAtPr(r, \beta, \delta, s, s') = p \equiv$$

if $\exists \alpha, p' . Choice(\beta, \alpha) \wedge$
 $transAtPr(r, \alpha, \delta, s, s') \cdot prob_0(\beta, \alpha, s) = p' \wedge p' > 0$
then $p = p'$ **else** $p = 0$

α outcome of β
 prob. of outcome α

Robustness: $transAtPr$

rest program

$$transAtPr(r, \alpha, \delta, s, s') = p \equiv$$

if $\exists^1 \tau . \tau \geq start(s) \wedge Poss(\alpha[s, \tau], s) \wedge s' = do(\alpha[s, \tau], s) \wedge$
 $(\forall \tau', s'' . \tau' \geq start(s) \wedge Poss(\alpha[s, \tau'], s) \wedge s'' = do(\alpha[s, \tau'], s) \supset$
 $value(r, \delta, s') \geq value(r, \delta, s''))$ choose r -maximizing τ
 then $p = 1$ else $p = 0$

$$transAtPr(r, \beta, \delta, s, s') = p \equiv$$

if $\exists \alpha, p' . Choice(\beta, \alpha) \wedge$ α outcome of β
 $transAtPr(r, \alpha, \delta, s, s') \cdot prob_0(\beta, \alpha, s) = p' \wedge p' > 0$ prob. of outcome α
 then $p = p'$ else $p = 0$

$$transAtPr(r, \phi?, \delta, s, s') = p \equiv$$

if $\phi[s] \wedge s' = s$ then $p = 1$ else $p = 0$.

Robustness: $transPr$

$$transPr(r, \sigma, s, \delta, s') = p \equiv$$

if $\exists^1 \gamma_1, \delta_1 . Next(\sigma, \gamma_1, \delta_1) \wedge$
 $(\forall \gamma_2, \delta_2 . Next(\sigma, \gamma_2, \delta_2) \supset$
 $value(r, (\gamma_1; \delta_1), s) \geq value(r, (\gamma_2; \delta_2), s))$
then (**if** $\delta = \delta_1$ **then** $p = transAtPr(r, \gamma_1, \delta_1, s, s')$ **else** $p = 0$)
else $p = 0$

decomposition $\gamma_1; \delta_1$ is optimal
 execute γ_1

Robustness: $transPr$ and $Trans$

new semantics

old semantics

different configurations

$$\mathcal{D} \cup \mathcal{C} \cup \mathcal{C}' \models (\exists \delta, s') Trans(\sigma, s, \delta, s') \supset$$

$$(\exists \delta, s', p)(transPr(r, \sigma, s, \delta, s') = p \wedge$$

$$(p > 0 \vee r(s') = 0))$$

$$\mathcal{D} \cup \mathcal{C} \cup \mathcal{C}' \models transPr(r, \sigma, s, \delta, s') > 0 \supset Trans(\sigma, s, \delta, s')$$

same configurations

Robustness: $transPr^*$

$$\begin{aligned}
 transPr^*(r, \sigma, s, \delta, s') &= p \stackrel{\text{def}}{=} \\
 \text{if } \exists p' . \forall f . & (\forall r', \sigma_1, s_0 . f(r', \sigma_1, s_0, \sigma_1, s_0) = 1) \wedge \\
 & (\forall r', \sigma_1, \delta_1, \delta_2, s_0, s_1, s_2, p_1, p_2 . \\
 & \quad p_1 > 0 \wedge f(r', \sigma_1, s_0, \delta_1, s_1) = p_1 \wedge \\
 & \quad p_2 > 0 \wedge transPr(r', \delta_1, s_1, \delta_2, s_2) = p_2 \supset \\
 & \quad f(r', \sigma_1, s_0, \delta_2, s_2) = p_1 \cdot p_2) \supset \\
 & f(r, \sigma, s, \delta, s') = p' \\
 \text{then } p = p' \text{ else } & p = 0
 \end{aligned}$$

Robustness: *Final*

$$\begin{aligned} \textit{Final}(r, \sigma, s) &\equiv \textit{MaybeFinal}(\sigma) \wedge \\ &\quad \textit{value}(r, \textit{Nil}, s) \geq \textit{value}(r, \sigma, s) \end{aligned}$$

Robustness: $doPr^*$

$$doPr(r, \sigma, s, s') = p \stackrel{\text{def}}{=} \\ \mathbf{if} \exists p' . transPr^*(r, \sigma, s, s') = p' \wedge Final(r, \sigma, s') \wedge \\ (\forall s'')(s \sqsubseteq s'' \wedge s'' \sqsubset s' \supset \neg Final(r, \sigma, s'')) \\ \mathbf{then} p = p' \mathbf{else} p = 0$$

Atomic Complex Actions: Semantics

$$\text{Next}(\text{atomic}(\sigma), \gamma, \delta) \equiv \gamma = \text{atomic}(\sigma) \wedge \delta = \text{Nil}.$$

$$\begin{aligned} \text{Next}'(\sigma, \gamma, \delta) \stackrel{\text{def}}{=} & \forall P. (\forall \sigma', \gamma', \delta'. \text{Next}(\sigma', \gamma', \delta') \supset P(\sigma', \gamma', \delta')) \wedge \\ & (\forall \sigma', \sigma'', \gamma', \gamma'', \delta', \delta''. \\ & \quad P(\sigma', \gamma', \delta') \wedge \gamma' = \text{atomic}(\sigma'') \wedge \\ & \quad \text{Next}(\sigma''; \delta', \gamma'', \delta'') \supset \\ & \quad P(\sigma', \gamma'', \delta'')) \supset \\ & P(\sigma, \gamma, \delta) \wedge (\forall \sigma') \gamma \neq \text{atomic}(\sigma') \end{aligned}$$

Atomic Complex Actions: Plan Recognition

Candidate program:

- ▶ Make db inconsistent at $\tau_2 = 2$
- ▶ Regain consistency at $\tau_3 = 2$

Observations:

- ▶ $\tau_1 = 1$: $\phi_1 =$ "db cons."
- ▶ $\tau_2 = 2$: $\phi_2 =$ "db incons."
- ▶ $\tau_3 = 2$: $\phi_3 =$ "db cons."

Is (τ_2, ϕ_2) observable? **No!**

Inconsistent situation has timespan zero

Atomic Complex Actions: Plan Recognition

Candidate program:

- ▶ Make db inconsistent at $\tau_2 = 2$
- ▶ Regain consistency at $\tau_3 = 2$

Observations:

- ▶ $\tau_1 = 1$: $\phi_1 =$ “db cons.”
- ▶ $\tau_2 = 2$: $\phi_2 =$ “db incons.”
- ▶ $\tau_3 = 2$: $\phi_3 =$ “db cons.”

Should $observe(\tau_2, \phi_2)$ be executable? **No! But it is!**

```

 $\sigma \parallel ( \dots ;$ 
    atomic(observe( $\tau_2, \phi_2$ ); waitFor(now >  $\tau_2$ ));
     $\dots )$ 

```